

## errors, uncertainties, ...

“big picture”:



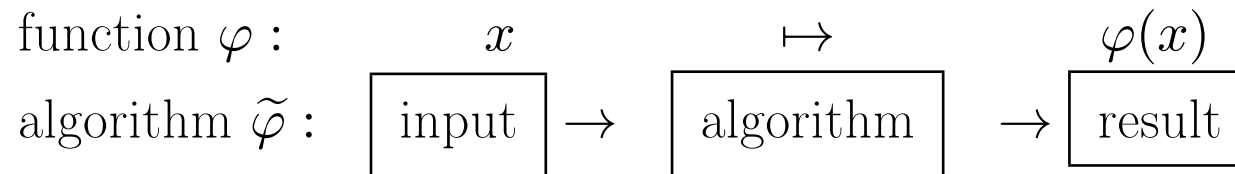
(A) sources of error “beyond” numerics:

- modelling errors & simplifications (e.g., Newtonian mechanics vs. relativity theory)
- data errors (models often contain parameter that are measured)

(B) sources of error numerics is “responsible” for:

- **discretization errors** (e.g., errors in quadrature formulas, stopping error in iterative zero-finding algorithms)
- **rounding errors** (effect of floating point arithmetic)

## conditioning and stability



- **conditioning of a function**  $\varphi$  measures how errors/perturbations in the input data affect the result. For poorly conditioned  $\varphi$  one **cannot** expect to be able to design good algorithms  $\tilde{\varphi}$ .
- **stability of an algorithm**  $\tilde{\varphi}$  measures how the algorithm influences perturbations in the input data. Numerics aims at **stable** algorithms.

simplistically:

- **conditioning** of a problem tells one whether it is at all possible to evaluate (on a computer) a function  $\varphi$
- **stability assesses** algorithms and is used as a selection criterion for algorithms